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# High Frequency Resonance Damping of DFIG based Wind Power System under Weak Network

Yipeng Song, Xiongfei Wang, *Member, IEEE*, and Frede Blaabjerg, *Fellow, IEEE*

**Abstract**—When operating in a micro or weak grid which has a relatively large network impedance, the Doubly Fed Induction Generator (DFIG) based wind power generation system is prone to suffer high frequency resonance due to the impedance interaction between DFIG system and the parallel compensated network (series  $RL$  + shunt  $C$ ). In order to improve the performance of the DFIG system as well as other units and loads connected to the weak grid, the high frequency resonance needs to be effectively damped. In this paper, the proposed active damping control strategy is able to implement effective damping either in the Rotor Side Converter (RSC) or in the Grid Side Converter (GSC), through the introduction of virtual positive capacitor or virtual negative inductor to reshape the DFIG system impedance and mitigate the high frequency resonance. A detailed theoretical explanation on the virtual positive capacitor or virtual negative inductor has been given, and their parameters are also optimally designed. The proposed DFIG system damping control strategy has been validated by experimental results.

**Index Terms** — DFIG system impedance; series  $RL$  + shunt  $C$  network; high frequency resonance damping; virtual positive capacitor; virtual negative inductor.

## I. INTRODUCTION

As the renewable power generation continues to increase worldwide, the penetration of wind energy, solar energy and etc. into the micro grid or weak grid is becoming more and more popular. Among the different kinds of renewable power generation units, the Doubly Fed Induction Generator (DFIG) based wind power generation has been widely implemented due to its performance advantages of a smaller converter rating around 30% of the generator rating, variable speed and four-quadrant active and reactive power operation capabilities, lower converter cost and power losses [1]-[6].

So far, the increasing number of renewable power generation units has been connected to the distributed weak network whose network impedance is much larger than the traditional large scale stiff power grid. As a consequence, the impedance interaction between the renewable power generation units (e.g., grid connected converter for solar energy, DFIG based wind turbine system) and the weak network requires careful considerations. Two kinds of resonances have been investigated in the previous works, i.e., the Sub- Synchronous Resonance (SSR) of the DFIG system [7]-[14] and high frequency resonance in the grid connected converter [15]-[23].

On one hand, the SSR phenomenon between the DFIG system and series compensated weak network has been well investigated based on the detail impedance modeling of DFIG system in [7]-[14]. The harmonic linearization method is employed to obtain the positive and negative impedance sequences of DFIG system in [7]-[10], especially the influence of PI regulator parameters in the rotor current

closed-loop control and phase locked loop control is studied concerning the SSR, and the DFIG SSR under different rotor speed is also investigated in [7]-[10]. Besides, the overall equivalent circuit modelling of the DFIG system and series compensated weak network is reported in [11], and it is concluded that the interaction between the electric network and the converter controller is a leading cause of the SSR phenomena. The design of auxiliary SSR damping controller and selection of control signals in the DFIG converters are demonstrated in [14] in order to effectively mitigate the SSR.

On the other hand, as for the grid-connected converter, many effective resonance damping strategies for the high frequency resonance have been reported in [15]-[24]. The active damping of high frequency resonance as well as the mitigation of harmonic distortion in the grid-connected converter is well investigated in [15]-[24]. The converter with series LC filter, rather than the traditional LCL filter, is studied to achieve the active damping in [16]. The virtual RC impedance is introduced in [18]-[19], i.e., positive resistance to achieve better performance of harmonic resonance damping; while negative inductance to achieve better performance of harmonic distortion mitigation by reducing the grid side inductance. The unknown resonance frequency is first identified by cascaded adaptive notch filter structure in [22], then the active damping can be implemented based on the detected resonance frequency. An overview of the virtual impedance based active damping strategy for the grid-connected voltage source and current source converters are summarized in [23], and several alternative methods of implementing the virtual impedance are concluded. Importantly, the interaction coupling between two converters connected to the same Point of Common Coupling (PCC) or different point of coupling via non-ideal grid is discussed in [24], and the bifurcation boundaries are also derived. Since the converter control parameters may influence its stability, a systematic design method of the controller parameter is given based on the chosen LCL filter resonance frequency in [25]-[26].

Thus, it can be found that the DFIG SSR and grid-connected converter high frequency resonance damping have been completely well investigated, while the case of DFIG high frequency resonance and its effective damping control strategy is never investigated before. In this paper, the active damping control strategy of the DFIG system high frequency resonance will be explored in detail, with the introduction of positive capacitor or negative inductor as a virtual impedance, so as to reshape the DFIG system impedance and damp the high frequency resonance.

It should be noted that the series compensated network consisting of resistor inductor capacitor (RLC) in series is taken into consideration in the DFIG SSR analysis in [7]-[14], while the other types of network, e.g., series  $RL$ , series  $RL$  + shunt  $C$ , are not investigated concerning the DFIG system, but only discussed concerning the grid connected converter active damping in [15]-[26]. Besides, the DFIG GSC filter in [7]-[14] adopts L filter, however in the practical application where large power scale DFIG turbine around MW is widely

implemented, the GSC filter always adopts the LCL filter due to its better switching harmonics filtering performance than the L filter.

This paper is organized as follows, the impedance modeling of DFIG machine and RSC, together with the impedance modeling of GSC and LCL filter, is established first in Section II. The high frequency resonance between DFIG system and the parallel compensated network (series RL + shunt C) is theoretically analyzed in Section III. The proposed active damping control strategy with the introduction of positive capacitor or negative inductor as virtual impedance in either RSC or GSC is demonstrated in Section IV. The parameters design of the virtual impedance and the control block diagram are given out in Section V. The proposed active damping strategy of DFIG system high frequency resonance is validated by experimental results in Section VI. Finally, the

conclusion is given in Section VII.

## II. DFIG SYSTEM IMPEDANCE MODELING

The DFIG system impedance modeling has been well established in [7]-[14], nevertheless since the impedance modeling serves as a foundation for the active damping strategy, the DFIG system impedance modeling still needs to be described here. Importantly, the LCL filter with better switching harmonics filtering performance, rather than the L filter in [7]-[14], is adopted in this paper. Besides, the mutual inductance and the digital control delay of 1.5 sample period [15] caused by the voltage/current sampling and PWM update are taken into consideration in the impedance modeling in this paper.

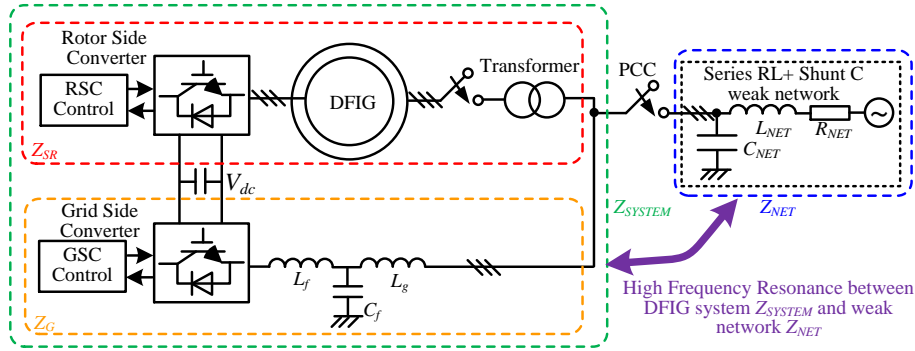


Fig. 1. Configuration diagram of the DFIG system and series RL + shunt C weak network

### A. General description of the investigated DFIG system

Fig. 1 shows the configuration diagram of the DFIG system and series RL + shunt C weak grid, the parameters of the DFIG system are available in Table I. As it can be seen, the RSC controls the rotor voltage to deliver the stator output active and reactive power, GSC is responsible for maintaining stable dc-link voltage, and the LCL filter is adopted due to better switching harmonic filtering performance. For the purpose of preventing grid connection inrush current and inner system current circulation, a transformer is connected between DFIG stator winding and PCC. The transformer does not change the voltage level between primary and secondary side, thus it will be neglected during the impedance modeling in following discussion.

### B. GSC and LCL filter impedance modeling

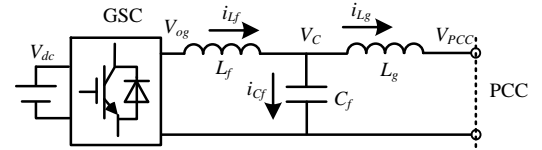


Fig. 2. Circuit of GSC and LCL filter

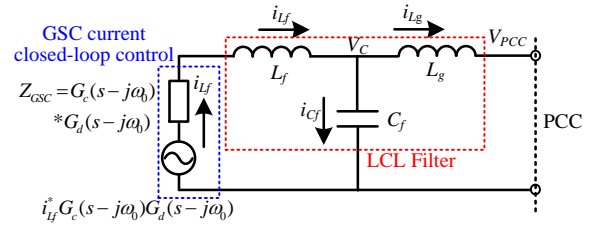


Fig. 3. Impedance modeling of GSC and LCL filter

As shown in Fig. 2, the grid side of DFIG system contains the GSC and the LCL filter. Based on [11], the impedance modeling of GSC and LCL filter can be presented in Fig. 3, where  $G_c(s-j\omega_0)$  is the PI current controller,  $G_d(s-j\omega_0)$  is the digital control delay of 1.5 sample period. Note that  $\omega_0$  is the grid network fundamental component angular speed of  $100\pi$  rad/s, it is introduced due to the implementation of PI closed-loop current regulation in the synchronous frame.

Normally, the GSC control has the outer control loop of the dc-link voltage, however since the dc-link voltage has much longer time constant, the control bandwidth of the dc-link voltage is lower than 100 Hz, thus the impedance modeling of the dc-link voltage control loop in the GSC is neglected.

Thus, as given in Fig. 3, the GSC current closed-loop control is modeled as one voltage source  $i_d^* G_c(s-j\omega_0) G_d(s-j\omega_0)$  in series connection with one impedance  $Z_{GSC} = G_c(s-j\omega_0) G_d(s-j\omega_0)$ .

According to the impedance theory, the impedance of the

TABLE I. PARAMETERS OF RSC, DFIG MACHINE, GSC AND LCL FILTER

Rated Power	7.5 kW	Voltage Level	400 V
$L_g$	7 mH	$L_f$	11 mH
$C_f$	6.6 $\mu$ F	$L_m$	79.3 mH
$L_{gs}$	3.44 mH	$L_{gr}$	5.16 mH
$R_s$	0.44 $\Omega$	$R_r$	0.64 $\Omega$
$K_{prsc}$	8	$K_{irsc}$	16
$K_{pgsc}$	8	$K_{igsc}$	16
$\omega_r$	0.8 p.u.	$T_d$	150 $\mu$ s
$f_s$	10 kHz	$f_{sw}$	5 kHz

The parallel compensated weak network with the configuration of series RL + shunt C is connected to the PCC. The high frequency resonance will occur through the impedance interaction between DFIG system and parallel compensated weak network, the detailed theoretical analysis can be found in following discussion.

GSC and LCL filter seen from the PCC can be obtained by setting the voltage source to zero, then the impedance of the DFIG grid side (including GSC and LCL filter) can be deduced as,

$$Z_G = \frac{Z_{Cf}(Z_{Lf} + Z_{GSC}) + Z_{Lg}(Z_{Lf} + Z_{GSC}) + Z_{Cf}Z_{Lg}}{Z_{Cf} + (Z_{Lf} + Z_{GSC})} \quad (1)$$

where,  $Z_{GSC} = G_c(s-j\omega_0)G_d(s-j\omega_0)$ ,  $Z_{Cf} = 1/sC_f$ ,  $Z_{Lf} = sL_f$ ,  $Z_{Lg} = sL_g$ .

### C. RSC and machine impedance modeling

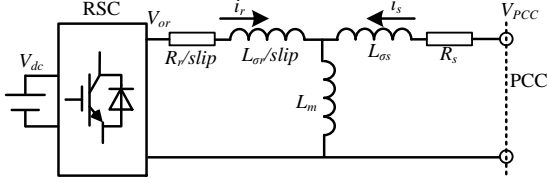


Fig. 4. Circuit of rotor side converter and DFIG machine

Fig. 4 shows the circuit of the RSC and DFIG machine. Since the rotor current control and output voltage are both calculated in the rotor stationary reference frame, they need to be rotated back to the stationary frame by the slip angular speed expressed as [7]-[10],

$$\text{slip} = (s - j\omega_r)/s \quad (2)$$

where,  $\omega_r$  is the rotor electric angular speed.

Similar as the GSC and LCL filter, the impedance modeling of RSC and DFIG machine can be obtained as shown in Fig. 5.

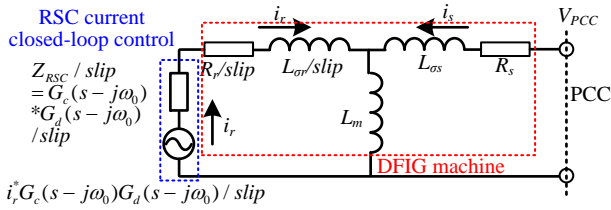


Fig. 5. Impedance modeling of rotor side converter and DFIG machine

By setting the rotor control voltage source to zero, the impedance of the RSC and DFIG machine seen from the PCC can be obtained as,

$$Z_{SR} = \frac{Z_{Lm}H/slip + (R_s + Z_{L\sigma s})H/slip + Z_{Lm}(R_s + Z_{L\sigma s})}{Z_{Lm} + H/slip} \quad (3)$$

where,  $H = R_r + Z_{L\sigma r} + Z_{RSC}$ ;  $Z_{RSC} = G_c(s-j\omega_0)G_d(s-j\omega_0)$ ;  $Z_{Lm} = sL_m$ ;  $Z_{L\sigma r} = sL_{\sigma r}$ ;  $Z_{L\sigma s} = sL_{\sigma s}$ .

### D. DFIG system impedance

As shown in Fig. 1, the rotor part (RSC and DFIG machine) and grid part (GSC and LCL filter) are connected in parallel to the PCC. Thus, the DFIG system impedance can be derived based on (1) and (3) as,

$$Z_{SYSTEM} = \frac{Z_G Z_{SR}}{Z_G + Z_{SR}} \quad (4)$$

The Bode diagrams of RSC and DFIG machine impedance  $Z_{SR}$ , GSC and LCL filter impedance  $Z_G$  and DFIG system impedance  $Z_{SYSTEM}$  are drawn in Fig. 6. The parameters used to plot the Bode diagram are given in Table I.

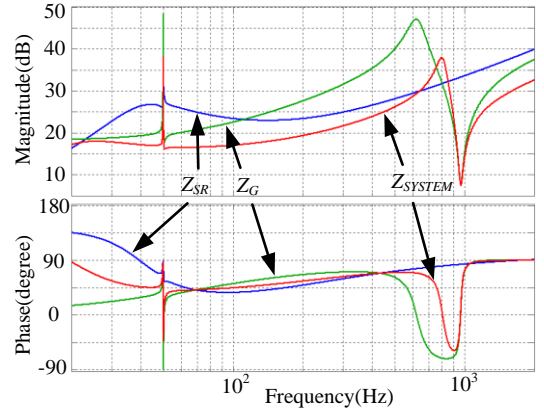


Fig. 6. Bode diagram of RSC and DFIG machine impedance  $Z_{SR}$ , GSC and LCL filter impedance  $Z_G$  and DFIG system impedance  $Z_{SYSTEM}$

As it can be observed from Fig. 6, within the lower frequency range, both the RSC and DFIG machine impedance  $Z_{SR}$  and GSC and LCL filter impedance  $Z_G$  have a high peak at 50 Hz due to the rotation of the reference frame from synchronous frame to stationary frame, thus the DFIG system impedance  $Z_{SYSTEM}$  also has the high peak at 50 Hz.

As for the higher frequency range (e.g., above 500 Hz), the  $Z_{SR}$  behaves almost as an inductive unit with the phase response about  $90^\circ$ . The  $Z_G$  has one magnitude peak around 620 Hz and one magnitude concave around 966 Hz caused by the LCL filter. It needs to point out the phase response of  $Z_G$  from 620 Hz and 966 Hz are capacitive below  $0^\circ$ , which is quite different from the  $Z_{SR}$ .

The DFIG system impedance  $Z_{SYSTEM}$  has a similar magnitude and phase response as the  $Z_G$ . However, due to the involvement of  $Z_{SR}$ , the  $Z_{SYSTEM}$  magnitude peak shifts from 620 Hz to 803 Hz, and the phase response within the range of 803 Hz to 966 Hz is also lifted up, which is helpful to avoid the high frequency resonance (will be explained in following sections).

## III. HIGH FREQUENCY RESONANCE BETWEEN DFIG SYSTEM AND PARALLEL COMPENSATED NETWORK

As explained in Fig. 6, the DFIG system behaves inductive with phase response of  $90^\circ$  at high frequency ( $> 1$  kHz), thus in order to make the high frequency resonance to happen, the weak network should behave capacitive with the phase response of  $-90^\circ$  at the high frequency, thus the phase difference of  $180^\circ$  will be produced to cause the high frequency resonance. From this point of view, the following discussion on the high frequency resonance between DFIG system and weak network will be conducted on the assumption of parallel compensated weak network, i.e., series RL+ shunt C network.

While for the series RL network which behaves inductive in the entire frequency range, it is impossible to make the high frequency resonance to occur because of almost zero phase difference between series RL weak network and DFIG system. For the series compensated network, i.e., series RLC network in [7]-[14], its phase response at high frequency is identical to series RL network, resulting in no high frequency resonance as well. Thus, the weak network configuration of series RL and series RLC will not be discussed in this paper.

Obviously, the impedance of the series RL + shunt C network can be presented as,

$$Z_{NET\_RL\_C} = \frac{(sL_{NET} + R_{NET}) \frac{1}{sC_{NET}}}{sL_{NET} + R_{NET} + \frac{1}{sC_{NET}}} \quad (5)$$

where,  $R_{NET}$  and  $L_{NET}$  are the network series resistance and inductance,  $C_{NET}$  is the network shunt capacitance.

The following equation can be obtained by rewriting the impedance of series  $RL$  + shunt  $C$  network in (5),

$$Z_{NET\_RL\_C} = \frac{\frac{1}{C_{NET}}s + \frac{R_{NET}}{L_{NET}C_{NET}}}{s^2 + \frac{R_{NET}}{L_{NET}}s + \frac{1}{L_{NET}C_{NET}}} \quad (6)$$

It can be observed from (6) that the magnitude peak of the network impedance is determined by  $L_{NET}$  and  $C_{NET}$ . In this paper the  $L_{NET}$  is assumed to be constant, while the  $C_{NET}$  will vary according to different compensation level, thus resulting in the network impedance peak to shift within certain frequency range.

As shown in Fig. 6, the phase response of DFIG system impedance is close to  $90^\circ$  at the frequency higher than 1 kHz. Therefore, the high frequency resonance is most likely to happen within the frequency range higher than 1 kHz, this will be described in details in the following discussion.

Fig. 7 shows the Bode diagram of the DFIG system impedance and series  $RL$  + shunt  $C$  network impedance with  $C_{NET}$  smaller than  $27 \mu F$  ( $27 \mu F$ ,  $24 \mu F$ ,  $21 \mu F$ ,  $18 \mu F$ ). As shown clearly, the network impedance and DFIG system impedance have several magnitude intersection points both in Zone 2 and Zone 1.

For the intersection points located within Zone 2, the phase differences are from  $135^\circ$  to  $149^\circ$ , indicating that the resonance from 800 Hz to 966 Hz is less likely to happen due to an acceptable phase margin, and the DFIG system can still work stable. On the other hand, for the intersection points located within Zone 1, the phase differences are always  $180^\circ$  for all the four cases of different capacitances, indicating that the high frequency resonance of 1160 Hz, 1220 Hz, 1290 Hz and 1380 Hz will occur respectively for the shunt capacitor  $C_{NET}$  of  $27 \mu F$ ,  $24 \mu F$ ,  $21 \mu F$ ,  $18 \mu F$ .

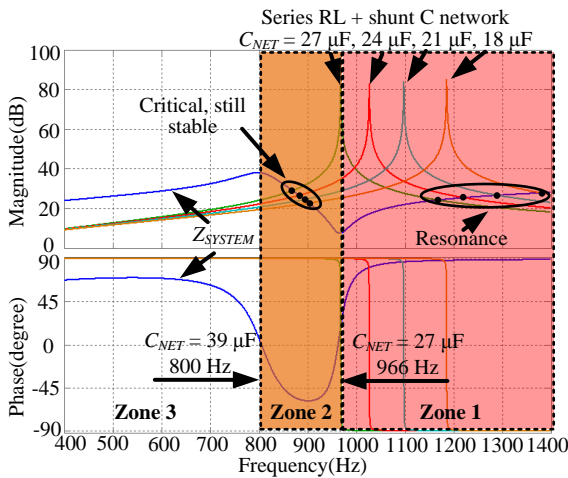


Fig. 7. Bode diagram of DFIG system impedance and series  $RL$  + shunt  $C$  network impedance with  $C_{NET}$  smaller than  $27 \mu F$  ( $27 \mu F$ ,  $24 \mu F$ ,  $21 \mu F$ ,  $18 \mu F$ ),  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1 \text{ mH}$

#### IV. PROPOSED ACTIVE DAMPING STRATEGY FOR DFIG SYSTEM

As illustrated in the previous section, the high frequency

resonance of 1220 Hz will happen if the DFIG system parameters are as listed in Table I, and the parallel compensated weak network parameters are chosen as  $C_{NET} = 24 \mu F$ ,  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1 \text{ mH}$ . In order to effectively damp the resonance, the virtual positive capacitor or negative inductor needs to be employed as explained in this section.

##### A. DFIG system impedance reshaping through RSC

As it can be seen from Fig. 7, for the sake of mitigating the high frequency resonance, the phase difference between the DFIG system and weak network needs to be reduced, obviously a concave in the phase response of DFIG system is preferred. Since the DFIG system behaves inductive at the high frequency range, the virtual positive capacitor or negative inductor is preferred due to their negative phase character.

In order to reshape the magnitude and phase response at only the resonance frequency rather than the entire frequency range, the resonant regulator can be employed due to its significant frequency selection capability [18].

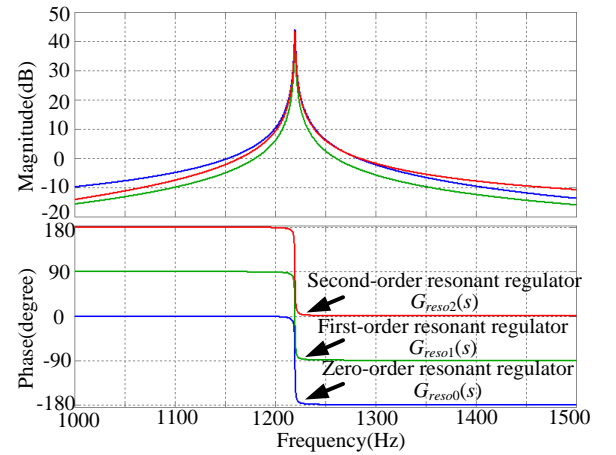


Fig. 8. Bode diagram of zero-order, first-order and second-order resonant regulator

$$G_{reso0}(s) = \frac{k_0}{s^2 + \omega_c s + \omega_{reso}^2} \quad (7a)$$

$$G_{reso1}(s) = \frac{k_1 s}{s^2 + \omega_c s + \omega_{reso}^2} \quad (7b)$$

$$G_{reso2}(s) = \frac{k_2 s^2}{s^2 + \omega_c s + \omega_{reso}^2} \quad (7b)$$

The Bode diagrams of three different resonant regulators, i.e., zero-order, first-order and second-order resonant regulator, are plotted in Fig. 8, and their transfer function presented in (7). As shown, the phase response changes from  $0^\circ$  to  $-180^\circ$  for zero-order resonant regulator,  $90^\circ$  to  $-90^\circ$  for first-order resonant regulator, and  $180^\circ$  to  $0^\circ$  for second-order resonant regulator respectively. This inherent character, i.e., phase response changing  $180^\circ$  at the tuned resonant frequency, obviously results in the opposite signs of the virtual impedance. For instance, when the positive capacitor and the zero-order resonant regulator are employed, the introduced capacitor will behave as positive capacitor due to the  $0^\circ$  phase response within the frequency range lower than resonant frequency, while behaves as a negative capacitor due to the  $180^\circ$  phase response within the frequency range higher than resonant frequency. The other cases can be similarly deduced.

Considering that the parallel compensated network has impedance shape of gradual decreasing magnitude as shown in Fig. 7, when the high frequency resonance frequency is



higher than 1 kHz, the reshaped impedance of the DFIG system is preferred to first decrease when lower than the resonance frequency, then increase when higher than the resonance frequency. By reshaping the DFIG system impedance like this, it can be ensured that only one magnitude intersection point, rather than three points, exists, and helps to reduce the possibility of high frequency resonance. The reason for reshaping the DFIG system impedance like this will be further explained in Fig. 10.

It should be noted that even the three different types (zero-, first-, second-order) of resonant regulators are plotted in Fig. 8, the first-order resonant regulator has been widely adopted [18] due to its significant frequency selection capability, thus it will be employed here to build the virtual impedance.

Based on above descriptions, the virtual impedance for DFIG system high frequency resonance damping can be obtained with the first-order resonant regulator and virtual components as the following,

1. Positive capacitor + first-order resonant regulator, equals to, positive zero-order virtual impedance
2. Negative inductor + first-order resonant regulator, equals to, negative second-order virtual impedance

**CASE 1.** Positive capacitor + first-order resonant regulator, equals to, positive zero-order virtual impedance

As illustrated above, the positive capacitor manages to reduce the magnitude of the DFIG system impedance which behaves as an inductance unit. By combining the first-order resonant regulator together with the positive capacitor, the positive zero-order virtual impedance can be obtained. It needs to point out that, as plotted in Fig. 8, the proposed virtual impedance behaves as a positive capacitor within the frequency range lower than resonant frequency due to the  $0^\circ$  phase response, while it behaves as a negative capacitor within the frequency range higher than resonant frequency due to the  $-180^\circ$  phase response.

The proposed virtual impedance with positive capacitor and first-order resonant regulator can be expressed as,

$$Z_{PC}(s) = \frac{\omega_c s}{s^2 + \omega_c s + \omega_{reso}^2} \frac{1}{s C_{xrsc}} = \frac{\omega_c / C_{xrsc}}{s^2 + \omega_c s + \omega_{reso}^2} \quad (8)$$

where,  $Z_{PC}$  is the proposed virtual impedance with virtual positive capacitor,  $C_{xrsc}$  is the proposed virtual positive capacitor,  $\omega_c$  is the resonant bandwidth parameter,  $\omega_{reso}$  is the resonant frequency.

Based on Fig. 5 and the positive capacitor + first-order resonant regulator virtual impedance, the reshaped impedance modelling can be obtained in Fig. 9. Since the  $Z_{PC}$  is implemented with the rotor current feedforward, the digital control delay and PWM update delay of total 1.5 sample periods also exists when introducing the virtual impedance. Inherently, this control delay is helpful to reduce the DFIG system phase response and increase the phase margin.

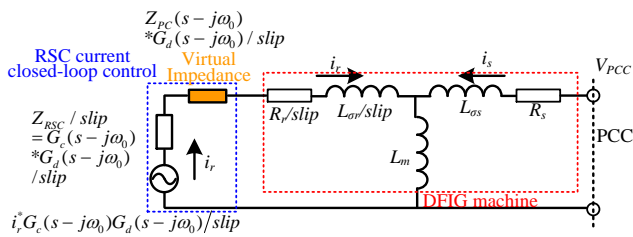


Fig. 9. Impedance modeling of RSC and DFIG machine with the introduction of virtual impedance

Thus, based on (8) and Fig. 9, the DFIG system impedance including the positive capacitor based virtual impedance in the RSC can be presented as,

$$Z_{SYSTEM\_SR\_PC} = \frac{Z_G Z_{SR\_PC}}{Z_G + Z_{SR\_PC}} \quad (9a)$$

$$Z_{SR\_PC} = \frac{Z_{Lm} H_{PC} / slip + (R_s + Z_{L\sigma s}) H_{PC} / slip + Z_{Lm} (R_s + Z_{L\sigma s})}{Z_{Lm} + H_{PC} / slip} \quad (9b)$$

where  $H_{PC} = R_r + Z_{L\sigma r} + Z_{RSC} + Z_{PC} G_d$ .

Bode diagram of DFIG system impedance  $Z_{SYSTEM\_SR\_PC}$  including the proposed virtual impedance  $Z_{SR\_PC}$  with positive capacitor and first-order resonant regulator is plotted in Fig. 10,  $\omega_c = 5$  rad/s,  $\omega_{reso} = 2\pi \cdot 1220$  rad/s,  $C_{xrsc} = 0.08$   $\mu$ F, control delay = 150  $\mu$ s. The control delay and slip are both taken into consideration in Fig. 10.

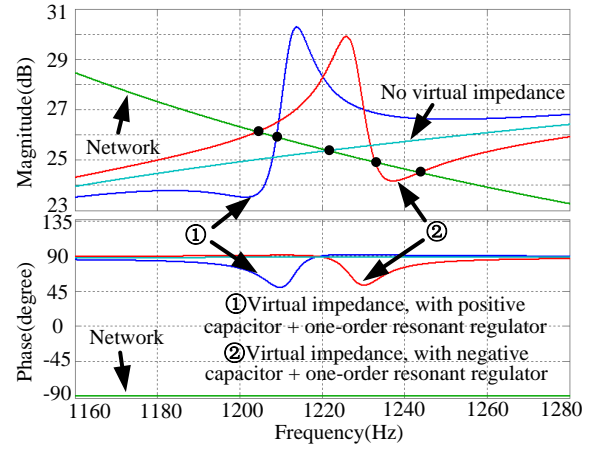


Fig. 10. Bode diagram of DFIG system impedance considering the proposed virtual impedance  $Z_{PC}$  with positive capacitor and first-order resonant regulator,  $\omega_c = 5$  rad/s,  $\omega_{reso} = 2\pi \cdot 1220$  rad/s,  $C_{xrsc} = 0.08$   $\mu$ F, control delay = 150  $\mu$ s.

As shown in Fig. 10, when no effective virtual impedance is introduced as shown in cyan, the DFIG system impedance has a magnitude intersection point with the weak network impedance at the frequency around 1220 Hz, and the corresponding phase difference is  $180^\circ$ , resulting in a high frequency resonance around 1220 Hz.

In contrast, when the virtual impedance of the positive capacitor is introduced in blue, the magnitude response of DFIG system first decreases, then increases, and at last decreases again. This impedance reshaping ensures that only one single magnitude intersection at around 1210 Hz exists, and the phase difference at 1210 Hz is effectively reduced to around  $142^\circ$ , which guarantees the effective damping of the high frequency resonance.

Nevertheless, if the negative capacitor is introduced, as shown in red, the magnitude response of the DFIG system first increases, then decreases, and at last increases again. As a result, there are three magnitude intersections at 1205 Hz, 1230 Hz and 1245 Hz respectively. As it can be observed, the intersection points at 1205 Hz and 1245 Hz may still unfortunately cause resonance. This unfavorable phenomenon can also be explained as, the proposed virtual negative capacitor behaves as inductive units at the frequency range lower than resonant frequency, thus the DFIG system impedance magnitude will first increase; then, the virtual negative capacitor behaves as capacitive units at the frequency range higher than resonant frequency, thus the DFIG system impedance magnitude will then decrease, just as shown in red in Fig. 10. Moreover, since the virtual negative capacitor behaves as capacitive units at the frequency range higher than

resonant frequency, the DFIG system impedance phase concave between 1220 Hz and 1240 Hz will be a consequence.

Thus, based on the above explanations, it can be found that the proposed virtual impedance of the positive capacitor + first-order resonant regulator is capable of appropriately reshaping the DFIG system impedance in order to mitigate the high frequency resonance.

**CASE 2.** Negative inductor + first-order resonant regulator, equals to, negative second-order virtual impedance

Obviously, the negative inductor has similar influence on the DFIG system impedance as the positive capacitor, the combination of negative inductor and first-order resonant regulator, which equals to the negative second-order virtual impedance, can be presented as,

$$Z_{NL}(s) = \frac{\omega_c s}{s^2 + \omega_c s + \omega_{reso}^2} * (-sL_{xrsc}) = \frac{-\omega_c L_{xrsc} s^2}{s^2 + \omega_c s + \omega_{reso}^2} \quad (10)$$

where,  $Z_{NL}$  is the proposed virtual impedance with negative inductor,  $-L_{xrsc}$  is the proposed negative inductor.

The similar impedance reshaping result as shown in Fig. 9 can be obtained and is not given here for the sake of simplicity. Based on (10) and Fig. 9, the DFIG system impedance including the negative inductor based virtual impedance in RSC can be presented as,

$$Z_{SYSTEM\_SR\_NL} = \frac{Z_G Z_{SR\_NL}}{Z_G + Z_{SR\_NL}} \quad (11a)$$

$$Z_{SR\_NL} = \frac{Z_{Lm} H_{NL} / slip + (R_s + Z_{L\sigma s}) H_{NL} / slip + Z_{Lm} (R_s + Z_{L\sigma s})}{Z_{Lm} + H_{NL} / slip} \quad (11b)$$

where,  $H_{NL} = R_r + Z_{L\sigma r} + Z_{RSC} + Z_{NL} G_d$ .

By adjusting the appropriate negative inductor value to fit the equation of  $1/(\omega_{reso} C_{xrsc}) = \omega_{reso} L_{xrsc}$ ,  $L_{xrsc} = 210$  mH, the same Bode diagram of the DFIG system impedance with virtual negative inductor can be obtained, thus it will not be repeated here for the sake of simplicity.

It is important to clarify that, the proposed virtual negative inductance value  $L_{xrsc}$  of 210 mH is reasonable and appropriate for the following two reasons. Firstly, the digital control delay of 1.5 sample period will cause the transformation of virtual negative inductance to the combination of virtual negative inductance and negative resistance, as a consequence, the amplitude of virtual negative inductance will be multiplied with  $\cos(\omega_{reso} T_d) = 0.4$ . Secondly, since the virtual negative inductance is implemented through rotor current feedforward, this means the virtual negative inductance is inserted in the DFIG rotor branch as shown in Fig. 9, thus the amplitude of virtual negative inductance should be close to the DFIG mutual inductance of 79 mH in order to have an distinctive influence on the DFIG system impedance. The detailed theoretical explanation about these two reasons can be found in the following section of virtual impedance parameters design.

Based on the above explanations, it can be found that the introduced virtual positive capacitor and negative inductor have the same influence on the DFIG system impedance from the perspective of impedance reshaping so as to mitigate the high frequency resonance.

## B. DFIG system impedance reshaping through GSC

Obviously, the abovementioned two different kinds of virtual impedance can also be employed in GSC to reshape the DFIG system impedance. The introduced virtual impedance based on the positive capacitor can be presented the same as (8) and will not be described here.

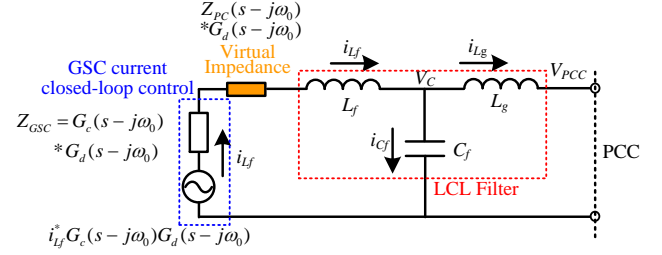


Fig. 11. Impedance modeling of GSC and LCL filter

Based on Fig. 11, the DFIG system impedance with the reshaped grid side impedance can be presented as,

$$Z_{SYSTEM\_G\_PC} = \frac{Z_{G\_PC} Z_{SR}}{Z_{G\_PC} + Z_{SR}} \quad (12a)$$

$$Z_{G\_PC} = \frac{Z_{Cf} (Z_{Lf} + Z_{GSC} + Z_{PC} G_d) + Z_{Lg} (Z_{Lf} + Z_{GSC} + Z_{PC} G_d) + Z_{Cf} Z_{Lg}}{Z_{Cf} + (Z_{Lf} + Z_{GSC} + Z_{PC} G_d)} \quad (12b)$$

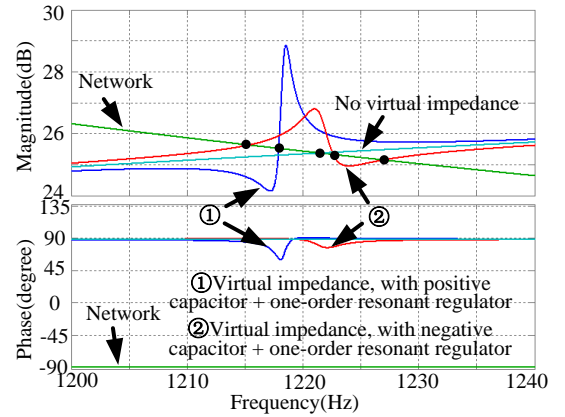


Fig. 12. Bode diagram of DFIG system impedance considering the proposed virtual impedance  $Z_{PC}$  with positive capacitor and first-order resonant regulator in GSC,  $\omega_c = 5$  rad/s,  $\omega_{reso} = 2\pi * 1220$  rad/s,  $C_{xgsc} = 0.5$   $\mu$ F, control delay = 150  $\mu$ s.

Fig. 12 shows the Bode diagram of the DFIG system impedance considering the proposed virtual impedance  $Z_{PC}$  with positive capacitor and first-order resonant regulator in the GSC,  $\omega_c = 5$  rad/s,  $\omega_{reso} = 2\pi * 1220$  rad/s,  $C_{xgsc} = 0.5$   $\mu$ F, control delay = 150  $\mu$ s.

The Bode diagram of (12) is very similar to Fig. 10. When the positive capacitor based virtual impedance is employed (in blue), the magnitude intersection point moves from 1220 Hz to 1217 Hz, and the phase difference also decreases from  $180^\circ$  to  $151^\circ$ . This means, through the effective impedance reshaping by the proposed virtual impedance in GSC, the original magnitude intersection point at 1220Hz with the phase response of  $180^\circ$  can be successfully moved to the new magnitude intersection point at 1217Hz with the phase response of  $151^\circ$ , thus the high frequency resonance can be effectively mitigated.

Nevertheless, if the negative capacitor is adopted (in red), three intersection points at 1215 Hz, 1223 Hz and 1227 Hz

occur, and the high frequency resonance of 1215 Hz and 1227 Hz are still seen.

Clearly, when the negative inductor, instead of the positive capacitor, is implemented, the high frequency resonance can also be successfully eliminated if the negative inductor value is appropriately tuned, thus it will not be described in detail here.

## V. VIRTUAL IMPEDANCE PARAMETERS DESIGN AND CONTROL BLOCK DIAGRAM

### A. Parameter design of virtual impedance for RSC and GSC implementation

In order to achieve satisfactory damping of the high frequency resonance, the parameter of the introduced virtual impedance needs to be carefully designed. The following discusses the positive capacitor and negative inductor parameter design for the RSC and GSC implementation.

#### 1. Parameter design of virtual impedance for RSC

As shown in Fig. 9, the implementation of virtual impedance in the RSC only influences the rotor branch, and the rotor branch is in parallel connection with the mutual inductance branch. Thus, the paralleled impedance of the rotor branch and mutual inductance branch can be presented as, (for the sake of clearer illustration, the negative inductor is taken as an example)

$$Z_{RM} = \frac{sL_m s(L_{\sigma r} - L_{xrsc} e^{-sT_d})}{s(L_m + L_{\sigma r} - L_{xrsc} e^{-sT_d})} \quad (13)$$

where, the rotor resistance is small enough to be neglected, and the PI current regulator which contains the  $k_p$  part as resistance, and  $k_i$  part as capacitance, can also be neglected due to its small value of  $k_p$  and  $k_i$ .

It is clear that in order to reshape the inherent inductive nature of DFIG system impedance, the  $Z_{RM}$  needs to become capacitive with its magnitude as large as possible, so the denominator of (13) needs to be as small as possible. According to the Euler equation, the denominator of (13) can be rewritten as,

$$\begin{aligned} L_m + L_{\sigma r} - L_{xrsc} e^{-sT_d} \\ = L_m + L_{\sigma r} - L_{xrsc} (\cos(\omega_{reso} T_d) - j \sin(\omega_{reso} T_d)) \end{aligned} \quad (14)$$

where,  $T_d$  is the digital control delay.

By assuming the following equation, the largest equivalent capacitive impedance of  $Z_{RM}$  in (13) can be obtained as,

$$L_{xrsc} = (L_m + L_{\sigma r}) / \cos(\omega_{reso} T_d) \quad (15)$$

By substituting the parameters given in Table I, the optimized value of the virtual impedance for RSC damping implementation can be calculated as a negative inductor of -206 mH (the reasons for this large inductance value is given below Fig. 10) or the positive capacitor of 0.08  $\mu$ F. This calculation result has been used to plot the Bode diagram of DFIG system impedance with the introduction of virtual impedance in Fig. 10, and it is shown that the original resonance of 1220 Hz can be well eliminated, and the magnitude intersection point shifts to 1210 Hz with the phase difference of 142°.

It can be also found from (15) that the optimized virtual impedance parameter for RSC is determined by mutual inductance  $L_m$ , rotor leakage inductance  $L_{\sigma r}$ , resonance frequency  $\omega_{reso}$  and control delay  $T_d$ .

#### 2. Parameter design of virtual impedance for GSC

Similar deduction can be adopted to obtain the optimized parameter of virtual impedance for the GSC.

According to Fig. 11, the implementation of virtual impedance in the GSC only influences the converter branch, and the filter capacitor is in parallel connection with the converter branch.

Thus, the paralleled impedance of the converter branch and the filter capacitor can be presented as, (for the sake of clearer illustration, the negative inductance is taken as an example),

$$Z_{GC} = \frac{\frac{1}{C_f} (L_f - L_{xgsc} e^{-sT_d})}{\frac{1}{sC_f} + s(L_f - L_{xgsc} e^{-sT_d})} \quad (16)$$

where, the PI current regulator which contains the  $k_p$  part as resistance and  $k_i$  part as capacitance can be neglected due to its small value of  $k_p$  and  $k_i$ .

In order to make the  $Z_{GC}$  a capacitive unit with its magnitude as large as possible, the denominator of (16) needs to be as small as possible. According to the Euler equation, the denominator of (16) can be rewritten as,

$$\begin{aligned} \frac{1}{sC} + s(L_1 - L_{xgsc} e^{-sT_d}) \\ = \frac{1}{sC} + s(L_1 - L_{xgsc} (\cos(\omega_{reso} T_d) - j \sin(\omega_{reso} T_d))) \end{aligned} \quad (17)$$

By assuming the following equation, the largest equivalent capacitive impedance of  $Z_{GC}$  in (16) can be obtained as,

$$L_{xgsc} = (L_1 - 1/\omega_{reso}^2 C) / \cos(\omega_{reso} T_d) \quad (18)$$

By substituting the parameters given in Table I, the optimized value of virtual impedance for GSC damping implementation can be calculated as a negative inductor of -34 mH or the positive capacitor of 0.5  $\mu$ F. This result has been used to plot the Bode diagram of DFIG system impedance with the introduction of virtual impedance in Fig. 12, and it is shown that the original resonance of 1220 Hz can be well eliminated, and the magnitude intersection point shifts to 1217 Hz with the phase difference of 151°.

It can be also found from (18) that the optimized virtual impedance parameter for GSC is determined by converter side inductor filter  $L_f$ , capacitor filter  $C_f$ , resonance frequency  $\omega_{reso}$  and control time delay  $T_d$ .

In conclusion, by comparing the reshaped DFIG system impedance with the virtual impedance as shown in Fig. 10 and Fig. 12, it can be found that the active damping in RSC with virtual impedance has a larger phase margin of 38° than the that of GSC with a virtual impedance of 29°, thus better high frequency resonance damping can be achieved if the virtual impedance damping is implemented in RSC control.

#### B. Control block diagram

Fig. 13 shows the control block diagram of the proposed DFIG system high frequency resonance damping control strategy using virtual impedance of Positive Capacitor (PC) or Negative Inductor (NL), and this strategy can be implemented in either RSC or GSC.

As it can be seen, for the RSC control, since the occurrence of DFIG system high frequency resonance will pollute the stator voltage with high frequency components higher than 1 kHz, an enhanced PLL module integrated with low-pass filter can be used to provide the information of grid voltage



fundamental synchronous angular speed  $\omega_1$  and phase angle  $\theta_1$ , while the encoder gives out the DFIG rotor position  $\theta_r$  and speed  $\omega_r$ . The rotor current  $I_{rdq}^+$  is first sampled and then regulated with PI regulator to output the harvested wind energy.

The resonance frequency detection unit employs an Adaptive Notch Filter (ANF) and Frequency-Locked Loop (FLL) to detect and output the resonance frequency  $\omega_{reso}$  [22]. The ANF unit is responsible to extract the resonance component, while the FLL unit is responsible to identify the frequency of the resonance component. Then, the proposed virtual impedance with positive capacitor or negative inductor can be flexibly adjusted based on various resonance frequencies. The introduction of virtual impedance does not require rotor current closed-loop control, but it can be regarded as rotor current feedforward component. Then, the

output of the rotor current PI closed-loop control  $V_{rdqPI}^+$ , the output of virtual impedance  $V_{rdqVI}^+$  and the decoupling compensation are added together as the rotor control voltage  $V_{rdq}^+$ , which is then transformed to the rotor stationary frame and delivered as an input of the Space Vector Pulse Width Modulation (SVPWM).

The GSC control can similarly be implemented as the RSC control. The dc-link voltage is well regulated by PI regulator, and its output is delivered as  $L_f$  filter current d-axis component reference  $I_{fd}^{*+}$ , then the  $L_f$  filter current  $I_{fdq}$  is regulated also by the PI regulator. The virtual impedance in the GSC can be similarly introduced, and no  $L_f$  filter current closed-loop is required for the virtual impedance introduction, but only the  $L_f$  filter current feedforward with the virtual impedance is needed.

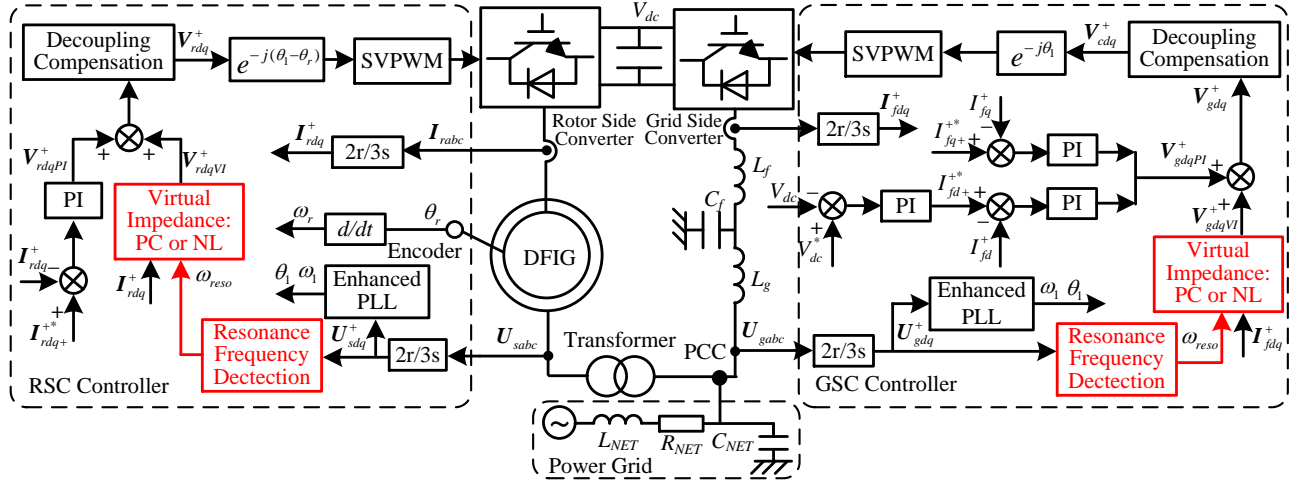


Fig. 13. Control block diagram of the proposed DFIG system high frequency resonance damping control strategy using virtual impedance of positive capacitor (PC) or negative inductor (NL)

## VI. EXPERIMENTAL VALIDATION

### A. Experimental setup

In order to validate the correctness of the proposed active damping strategy of DFIG system high frequency resonance implemented in either RSC or GSC, experimental setup is built up.

A down-scaled 7.5 kW test rig is used and the overall system is shown in Fig. 14. The experimental DFIG system parameters can be found in Table I. The weak network is simulated using three phase inductors and capacitors. The DFIG is externally driven by a prime motor, and two 5.5-kW Danfoss motor drives are used for the GSC and the RSC, both of which are controlled with dSPACE 1006. The rotor speed is set 1200 rpm (0.8 pu), with the synchronous speed of 1500 rpm (1.0 pu). The DFIG system output power is set at 5 kW. The dc-link voltage is 650

V. The sample frequency  $f_s$  and switching frequency  $f_{sw}$  for both RSC and GSC is 10 kHz and 5 kHz respectively. The weak network parameters are  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ ,  $C_{NET} = 10 \text{ }\mu\text{F}$ .

During the experimental validation process, the prime motor is driven by the general converter which will unfortunately inject high frequency switching noise to the power grid, as a consequence the  $u_g$  in all the experiment results Fig. 16 – Fig. 24 will contain switching noise due to the weak power grid impedance. This switching noise can be filtered out by the transformer leakage inductance, thus the stator voltage  $u_s$  in all the experiment results do not contain the noise. Considering that this noise does not influence the resonance active damping performance, the experimental results are still valid to validate the active damping method.

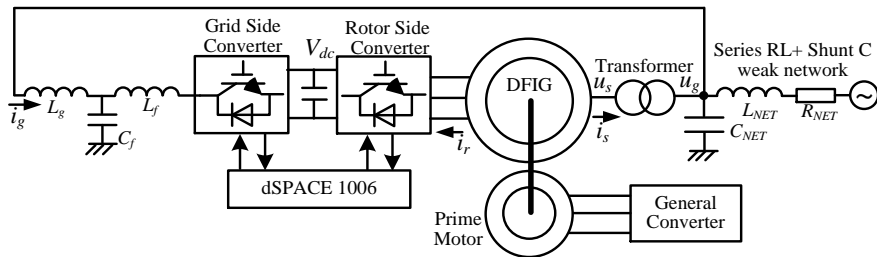


Fig. 14. Setup of 7.5 kW DFIG system test rig

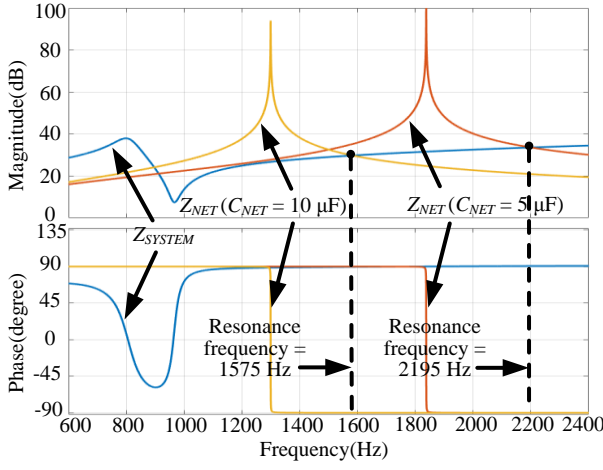


Fig. 15. Bode diagram of DFIG system impedance and series RL + shunt C network impedance with  $C_{NET}=10, 5 \mu\text{F}$ ,  $R_{NET}=3 \text{ m}\Omega$ ,  $L_{NET}=1.5 \text{ mH}$

The Bode diagrams of the DFIG system impedance and the parallel compensated weak network impedance ( $R_{NET}=3 \text{ m}\Omega$ ,  $L_{NET}=1.5 \text{ mH}$ ,  $C_{NET}=10, 5 \mu\text{F}$ ) are plotted in Fig. 15. As it can be seen, the theoretical analysis shows that the high frequency resonance of 1575 Hz and 2195 Hz will occur due to the phase difference of 180 between network impedance  $Z_{NET}$  and DFIG system impedance  $Z_{SYSTEM}$  when the network shunt capacitance  $C_{NET}=10, 5 \mu\text{F}$  respectively.

### B. Experimental results

Fig. 16 shows the experimental result of the DFIG system when no effective active damping control strategy is implemented. Clearly, the high frequency resonance around 1600 Hz, which matches well with the theoretical analysis

results shown in Fig. 15, will occur in three phase stator voltage and current, rotor current, grid side voltage and current as a consequence of impedance interaction between the DFIG system and the parallel compensated weak network grid.

Fig. 17 shows the experimental result of DFIG system when the proposed active damping control strategy is implemented in the RSC by the rotor current feedforward method. By comparing the experimental results shown in Fig. 16 and Fig. 17, it can be explicitly found that the high frequency resonance can be effectively damped in all the stator voltage and current, grid side voltage and current. Therefore, the effectiveness of the proposed active damping strategy implemented in the RSC can be validated based on the experimental results.

Moreover, the experimental result of transient response at the enabling instant of the active damping strategy in RSC is also provided in Fig. 18. As it can be observed, once the damping is enabled, the high frequency resonance components in the stator voltage and current, as well as the grid side voltage and current can be mitigated within around 10 ms, which verifies the fast dynamic response capability of the proposed active damping method.

TABLE II. HIGH FREQUENCY RESONANCE ACCORDING TO THEORETICAL ANALYSIS AND EXPERIMENTAL RESULTS

Shunt Capacitor	Theoretical Analysis	Experimental Results	
		Active damping disabled	Active damping enabled
10 $\mu\text{F}$	1575 Hz	1600 Hz $u_s$ , 28.5%	1600 Hz $u_s$ , 6.7%
5 $\mu\text{F}$	2195 Hz	2250 Hz $u_s$ , 38.7%	2250 Hz $u_s$ , 8.6%

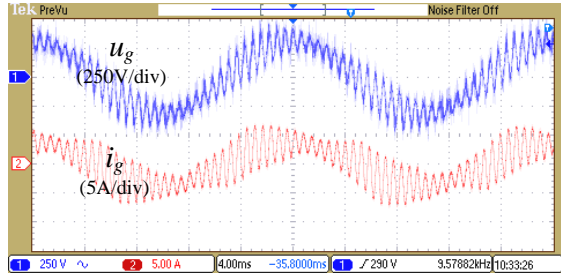
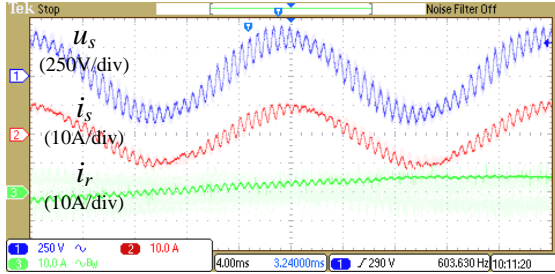


Fig. 16. No active damping strategy, weak network parameters of  $R_{NET}=3 \text{ m}\Omega$ ,  $L_{NET}=1.5 \text{ mH}$ ,  $C_{NET}=10 \mu\text{F}$

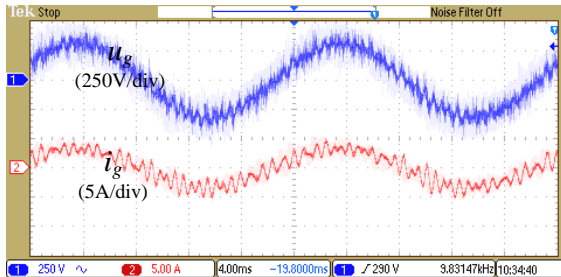
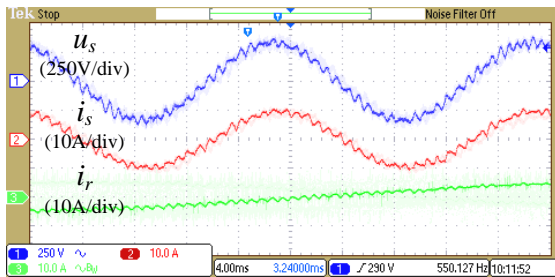


Fig. 17. Steady state response when active damping strategy in RSC is enabled, weak network parameters of  $R_{NET}=3 \text{ m}\Omega$ ,  $L_{NET}=1.5 \text{ mH}$ ,  $C_{NET}=10 \mu\text{F}$

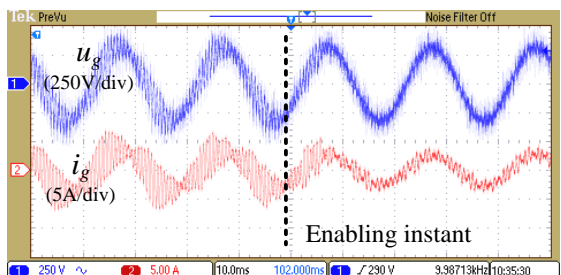
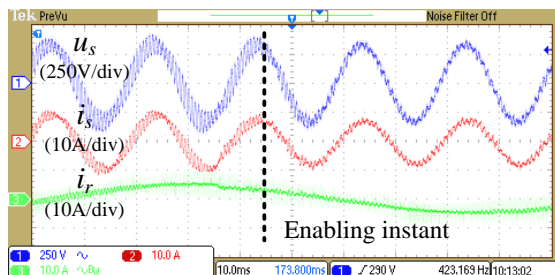


Fig. 18. Transient state response when active damping strategy in RSC is enabled, weak network parameters of  $R_{NET}=3 \text{ m}\Omega$ ,  $L_{NET}=1.5 \text{ mH}$ ,  $C_{NET}=10 \mu\text{F}$

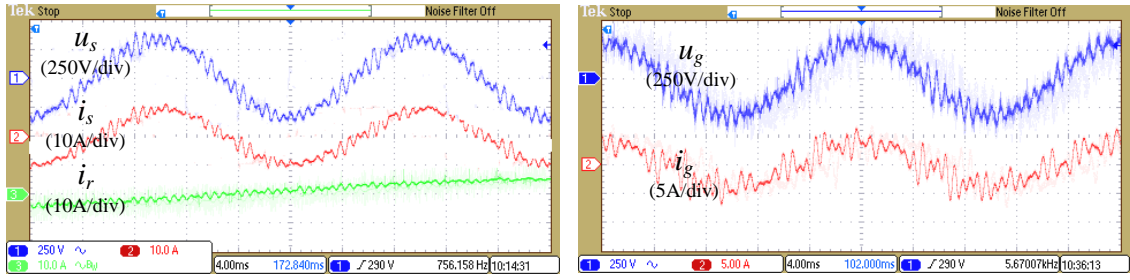


Fig. 19. Steady state response when active damping strategy in GSC is enabled, weak network parameters of  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ ,  $C_{NET} = 10 \text{ }\mu\text{F}$

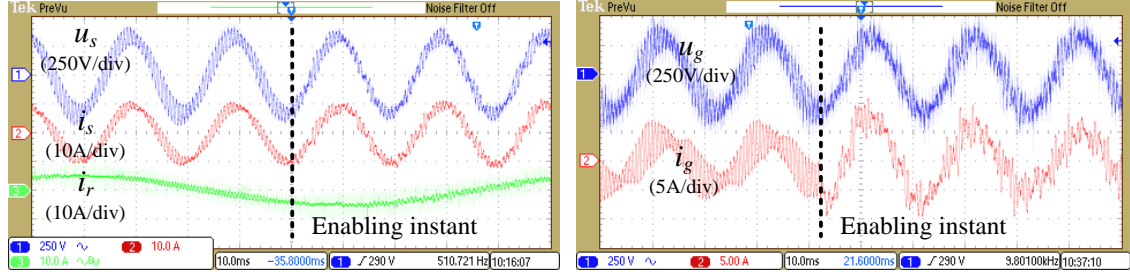


Fig. 20. Transient state response when active damping strategy in GSC is enabled, weak network parameters of  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ ,  $C_{NET} = 10 \text{ }\mu\text{F}$

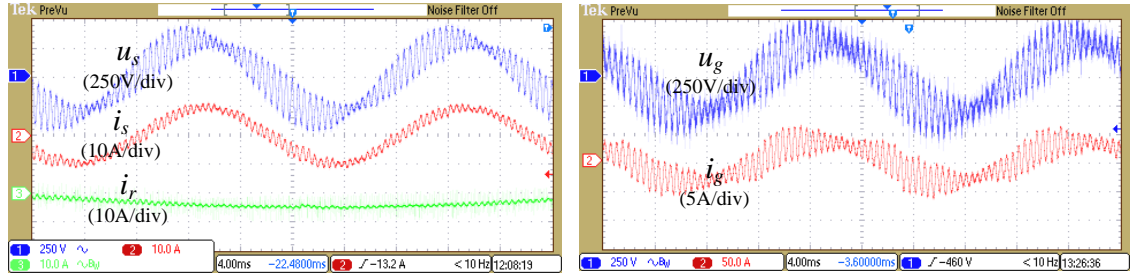


Fig. 21. Experimental result of DFIG system when shunt capacitance  $C_{NET} = 5 \text{ }\mu\text{F}$  in the weak grid network,  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ , no active damping strategy

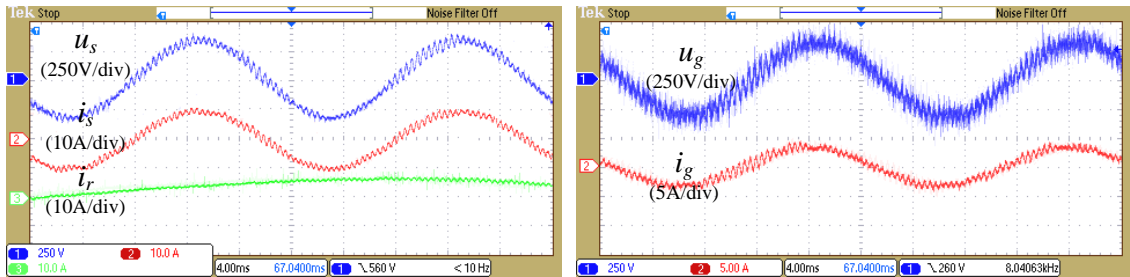


Fig. 22. Steady state response when active damping strategy in RSC is enabled, weak network parameters of  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ ,  $C_{NET} = 5 \text{ }\mu\text{F}$

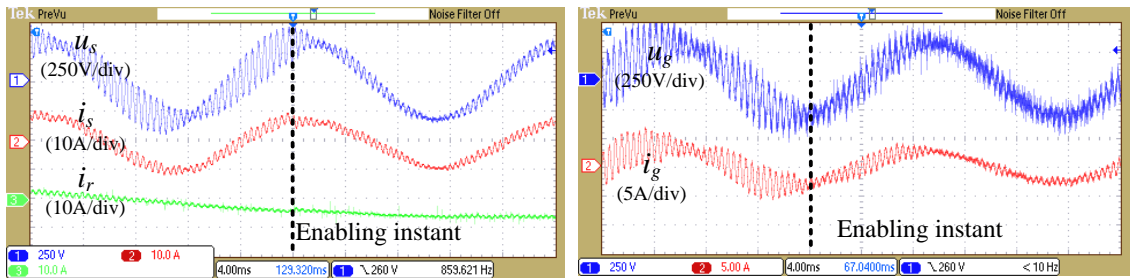


Fig. 23. Transient state response when active damping strategy in RSC is enabled, weak network parameters of  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ ,  $C_{NET} = 5 \text{ }\mu\text{F}$

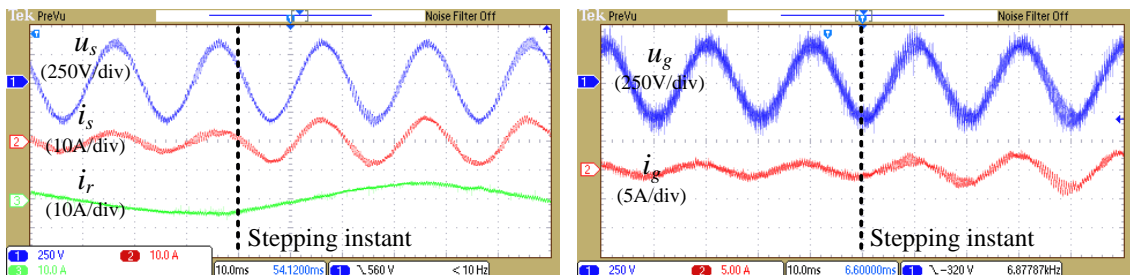


Fig. 24. Transient state response of DFIG stator output power stepping from 0.5 p.u. to 1.0 p.u. when active damping strategy in RSC is enabled, weak network parameters of  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ ,  $C_{NET} = 5 \text{ }\mu\text{F}$



Similarly, the active damping strategy can also be implemented in GSC, with the converter side current feedforward method. According to Fig. 19, when the active damping strategy in GSC is enabled, the high frequency resonance components can also be mitigated. However, it should be noted that the active damping performance when GSC is involved as shown in Fig. 19 is poorer than the active damping performance when the RSC is involved as shown in Fig. 17. According to the theoretical analysis conducted in Section IV, this difference is because that the RSC with the virtual impedance has a larger phase margin of  $38^\circ$  than the GSC with the virtual impedance of  $29^\circ$ , thus a better high frequency resonance damping can be achieved if the virtual impedance damping is implemented in RSC control, which validates the correctness of the analysis results given in Fig. 10 and Fig. 12.

Fig. 20 shows also the experimental result of transient response at the enabling instant of active damping strategy in the GSC. Similar as in Fig. 18, once the damping is enabled, the fast dynamic response of active damping can be achieved within around 10 ms, which also verifies the fast dynamic response capability of the proposed active damping strategy.

In order to further validate the effectiveness of the proposed active damping strategy, the experimental results under weak network parameters of  $R_{NET} = 3 \text{ m}\Omega$ ,  $L_{NET} = 1.5 \text{ mH}$ ,  $C_{NET} = 5 \text{ }\mu\text{F}$  are also provided. As a result of the network shunt capacitance changing from  $10 \text{ }\mu\text{F}$  to  $5 \text{ }\mu\text{F}$ , the high frequency resonance frequency changes from 1600 Hz to 2250 Hz as shown in Fig. 21, and this resonance frequency is also close to the theoretical analysis result of 2195 Hz in Fig. 15 and Table II.

Similarly, when active damping strategy in RSC is enabled as shown in Fig. 22, the resonance can be effectively mitigated both in stator voltage / current, rotor current and grid side current. Besides, the transient state response at the enabling instant of the active damping strategy in RSC is also given in Fig. 23, it can be observed that the active damping strategy is capable of mitigating the resonance within around 10 ms, which ensures its fast dynamic response capability.

Fig. 24 shows the transient response when the DFIG stator output active power steps from 0.5 p.u. to 1.0 p.u. Clearly, the active damping strategy remains effective within the entire stepping transient period, and the output active power steps within around 10 ms, which guarantees the excellent control capability of the delivered wind power to the grid. Most importantly, this experimental result is able to validate the effectiveness of the proposed damping strategy under practical application where the output wind power may always in variation.

Thus, based on the experimental results shown above, it can be concluded that, the proposed theoretical analysis on the high frequency resonance frequency is accurate, and the proposed active damping strategy implemented in either RSC or GSC is effective under practical application situation, i.e., under different weak network parameters (mainly with different network shunt capacitance in variation), as well as different stator output wind power, these advantages make the proposed active damping strategy reliable and effective in the real world wind power generation applications. Besides, the active damping strategy implemented in the RSC has a better performance than being implemented in GSC due to the larger phase margin, thus the active damping in RSC is preferred.

## VII. CONCLUSION

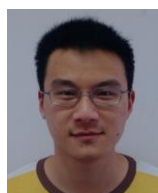
This paper has focused on the active damping control strategy for the DFIG system under parallel compensated weak network. The active damping strategy can be implemented in either RSC or GSC to reshape the overall DFIG system impedance.

- 1) The original high frequency resonance can be damped by decreasing the phase difference with the virtual negative capacitor or positive inductor to produce an acceptable phase margin.
- 2) The rotor current feedforward in the RSC and converter side current feedforward in GSC is proposed to introduce the virtual impedance and achieve the active damping performance.
- 3) Experimental results have validated the acceptable steady state active damping performance, and also the fast dynamic response capability of the proposed active damping strategy.
- 4) Both theoretical analysis and experimental results verify that better active damping performance can be ensured if the active damping strategy is implemented in the RSC rather than GSC.

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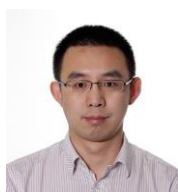
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